DEVELOPMENT OF THE PERFORMANCE PREDICTION ALGORITHMS FOR CLOUD SERVICES

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Abstract. Main stages of data center service performance prediction were discussed, specifically data monitoring and gathering, calculation and prediction of key indexes and performance index prediction. It was proposed to build data center service performance prediction algorithm based on an analysis of the service transactions index, service resource occupancy index and service performance index. Prediction of the indexes is based on chaotic time series analysis that was used to estimate service transactions index time series trend, the radar chart method to calculate the service resource occupancy index value and weighted average method to calculate service performance index. For performance prediction, it is proposed to use a fuzzy judgment matrix with the service transactions index and service resource occupancy index as input values. It was taken into consideration that service transactions index is usually represented by nonlinear time series and thus the index time series parameters had to be predicted by chaos theory and for the calculation of this index, the estimation procedure of Lyapunov exponent value can be used. The radar chart demonstrates service resource occupancy index estimation of shared storage, mobile storage, memory, computational capability and network bandwidth. The prediction technique was based on the fuzzy nearness category that use input values of transactions index and dynamic changes of the service resource occupancy index.

Keywords: data center, service transactions index, service resource occupancy index, service performance index, fuzzy judgment matrix, Lyapunov exponent, radar chart.

INTRODUCTION

Nowadays requirements to cloud platform data center services performance have significantly grown. Thereby it's important to develop effective and multipurpose algorithm of estimation of key aspects that refers to the stability of the network infrastructure work. An efficient strategy should be based on an analysis of the whole dataset of gathered information of a monitoring platform and to be able to predict indexes of the data center performance at any moment of time with the high accuracy.

The assigned task could be solved by mathematical methods of the chaotic analysis and fuzzy logic, but adaption of them stands a nontrivial task. In order to identify the main aspects of the problem, an analysis of recent studies and publi-

cations was done. It was analyzed that aspects of data center service performance that were mentioned to be key ones [1, 2], specifically service transactions index, service resource occupancy index and service performance index. To solve the problem of prediction of those, works were studied devoted to chaotic analysis [2-4], radar chart method [1, 5] and weighted average method [6]. Also, within the bounds of this study, the fundamental mathematical materials were analyzed [7–9] related to fuzzy logic in order to use it at cloud platform data center services performance analysis and prediction. The system analysis shows the possibility to develop an effective technique based on monitoring and gathering of information for estimation and accurate prediction of key aspects that refers to the data center service performance.

SERVICE INDEXES PREDICTION AND CALCULATION PROCEDURE

The data center service performance prediction procedure [1, 2] usually includes following stages (Fig. 1):
- monitoring and gathering of data center indicators' data;
- calculation and prediction of key indexes of data center infrastructure work;
- prediction of the data center service performance index.

Indicators' data contain recorded by virtual machine (VM) monitoring plugins information about transaction logs, utilization level of physical resources (shared storage, computational capability, network bandwidth, etc.) and response time of each monitoring spot which refers to the system performance. The analysis of gathered data allows defining key indexes of data center infrastructure work efficiency (Fig. 1):
- service transactions index (STI);
- service resource occupancy index (SROI);
- service performance index (SPI).

STI value refers to the number of data center's transactions that require a service to process. This index indicates service's loads at each moment and should be recorded as a time series $x_i : [x_1, x_2, ..., x_n]$ which corresponds to the time chart $t_i : [t_1, t_2, ..., t_n]$. As it is shown at Figure 1, usually STI time series have to be modeled as a nonlinear sequence. Thus, STI trends can be predicted by nonlinear time series forecasting methods based on the artificial neural networks (ANNs) platform. In other hand, SROI value refers to data center servers' physical resources allocated to the service at each moment and SPI value refers to the data center service's response time at each moment. It should be mentioned that SPI directly reflects service performance while this index is the comprehensive result of the key monitoring points' analysis.

Prediction of key indexes procedure includes a variety of methods or algorithms that can be used. Within the bounds of this study it is proposed to use (Fig. 1):
- chaotic time series analysis to estimate STI time series trend [2–4];
- radar chart method to calculate SROI value [1, 5];
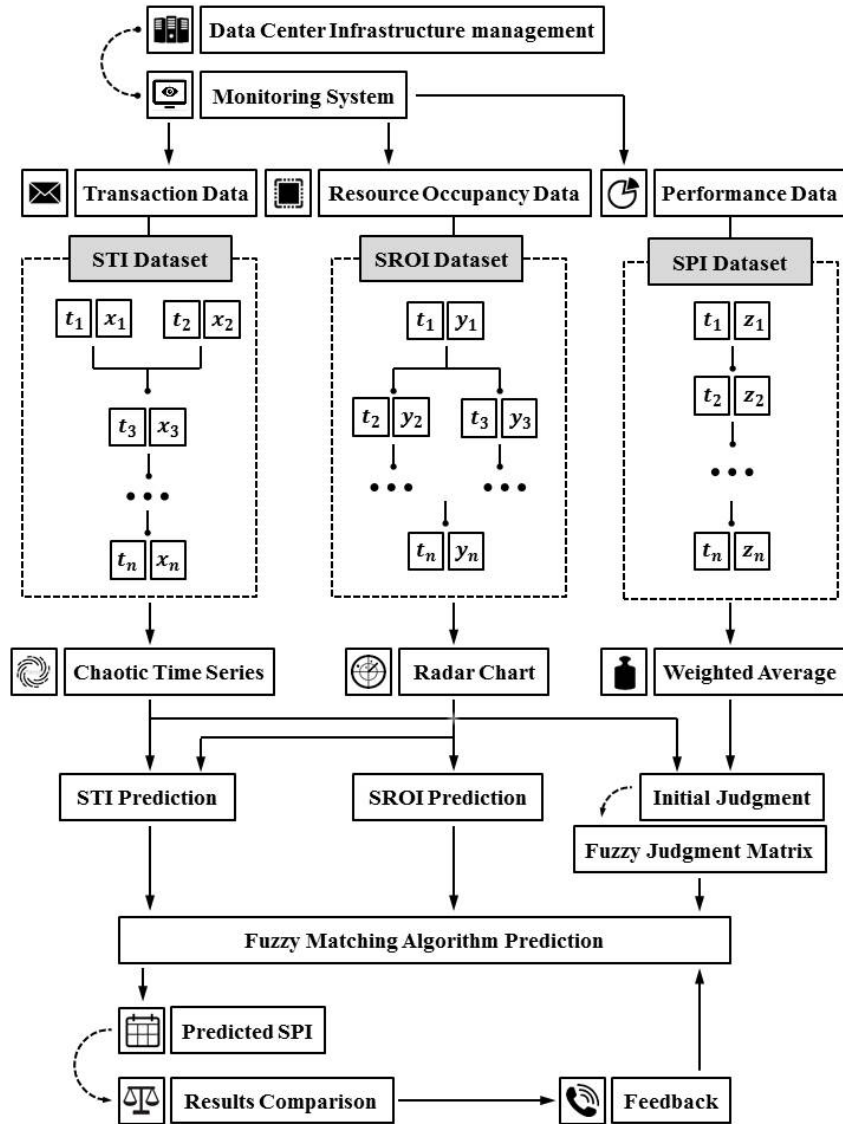- weighted average method to calculate SPI value [6].

Fig. 1. Data center service performance prediction scheme

Performance prediction of the modern data center service work process should be based on a fuzzy judgment matrix. It uses STI and SROI values (Figure 1) according to the definition of the fuzzy closeness degree, and estimate the best matching value of STI and SROI at the predicted moment by a similarity matching algorithm. Thereby, SPI which corresponds to the obtained value represents prediction result data center service performance to be compared with the value that was obtained experimentally.

STI TIME SERIES PREDICTION ALGORITHM

It was mentioned above that the modern data center service based on cloud paradigm is usually has to be represented by a nonlinear system. It could be added that

STI time series would be nonlinear time series on a cloud platform. Thereby, STI time series parameters have to be predicted by the chaos theory.

For reconstruction of STI time series the delay embedding theorem should be used (Takens' theorem). Let us suppose that time series $x_i : [x_1, x_2, \ldots, x_n]$ which corresponds to the time $t_i : [t_1, t_2, \ldots, t_n]$ have power system dimension d and thus the system must be considered form d-dimensional state vector $x_i(t)$ that evolves according to an unknown but continuous and deterministic dynamics. For simplified form of Takens' theorem [1, 7–9] adapted to the time series prediction it can be said that observable result F_x is a smooth function of x_i dataset. $F_x(t)$ has to be supplemented by observations made within certain time lag τ multiplied by values $k = 1, \ldots, m$:

$$F_x(t, k) : [F_x(t), F_x(t - \tau), F_x(t - 2\tau), \ldots, F_x(t - k\tau), \ldots, F_x(t - m\tau)].$$

It's obvious that for increasing number of lags m it will lead motion in the lagged space to become more predictable, and for $m \to \infty$ system will tend to become deterministic and equivalent to original state space. Takens' theorem [1] demonstrates that lagged vectors become deterministic at a finite dimension of $m \geq 2d + 1$. Thereby STI time series prediction's target function $F_x(t_i)$ of m-dimensional phase space with N phase points could be defined in every point in space phase as:

$$\begin{cases} F_x(t_i) = [x(t_i), x(t_i + \tau), x(t_i + 2\tau), \ldots, x(t_i + \tau(m-1))] \\ \qquad m \geq 2d + 1; \ i = 1, 2, \ldots, N; \ N = n - \tau(m-1). \end{cases}$$

It has to be noticed that $m \geq 2d + 1$ is not a necessary but sufficient condition of determination of system dynamics.

STI time series' calculation could be done not only by a qualitative analysis but also by a quantitative algorithm. It's based on calculating some chaotic quantities. The most effective way is to estimate Lyapunov exponent value. Lyapunov exponent of a dynamical system is a quantity that characterizes the rate of separation of infinitesimally close trajectories []. Two trajectories in phase space with initial separation δZ_0 diverge as:

$$\|\delta Z(t)\| \approx \|\delta Z_0\| \geq \lim_{\tau \to \infty} \left(\lim_{\delta Z_0 \to 0} \left(\frac{\ln \left(\frac{|\delta Z(t)|}{|\delta Z_0|} \right)}{t} \right) \right),$$

where λ is the Lyapunov exponent and $\delta Z_0 \to 0$ criteria ensure the validity of the linear approximation at each moment of time. Thereby, the biggest obtained value of Lyapunov exponent (MLE: maximal Lyapunov exponent) is a parameter which could be used for estimation whether a system is a chaotic one ($\lambda > 0$) or not ($\lambda \leq 0$). It should be noticed that the initial separation vector usually contain some component in the direction associated with the MLE, and thus an effect of the other exponents can be neglected.

For analysis of STI time series the proposed mathematical model could be slightly simplified. Let us suppose that we need to predict x_{n+k} for dataset of $x_i : [x_1, x_2, \ldots, x_n]$. We have to choose a point X_i for the prediction center in a phase space of the system. X_i is defined as:

$$X_i : [x_n - \tau(m-1), x_{n+1} - \tau(m-1), \ldots, x_{n+k} - \tau(m-1)].$$

The next step is to define nearest point $X_j : \{X_1, X_2, \ldots, X_{i-1}\}$. While distance between X_i and X_j is d, then d could be defined as $d = \|X_i - X_j\|$. Therefore, MLE could be estimated by comparison of $d = \|X_i - X_{i+1}\|$ and $\|X_j - X_{j+1}\|$ differences.

$$\|X_i - X_{i+1}\| = e^{\lambda_1} \|X_j - X_{j+1}\| \geq \lambda_1 = \ln\left(\frac{\|X_i - X_{i+1}\|}{\|X_j - X_{j+1}\|}\right).$$

While λ_1 is obtained MLE for time series $x_i : [x_1, x_2, \ldots, x_n]$, it predicts x_{n+1}. To predict x_{n+k}, k-step prediction should be done.

SROI AND SPI VALUE PREDICTION ALGORITHM

As it was mentioned above, SROI value refers to the data center service physical resources utilization level. Physical resources are distributed on different servers and VMs so estimation of SROI value is a nontrivial task. The most efficient method of SROI analysis is development of radar char, a graphical method of displaying multivariate data more than two quantitative variables [1, 5].

The radar chart area R(t) for SROI evaluation and prediction can be gotten as follows:

$$R(t) = \frac{\sin\left(\frac{2\pi}{3}\right)}{2} \sum_{i,j} [y_i y_j].$$

Fig. 2 shows the demonstrated radar chart that can be used for SROI analysis for five resources:
- shared storage;
- mobile storage;
- memory (RAM and cash-memory);
- computational capability (CPU);
- network bandwidth.

There are several methods of effective SPI prediction but all of them based on estimation of monitoring points response time dataset $T_i : [T_i \ldots T_n]$. Thereby, basic equation for SPI at any moment of time could be defined as:
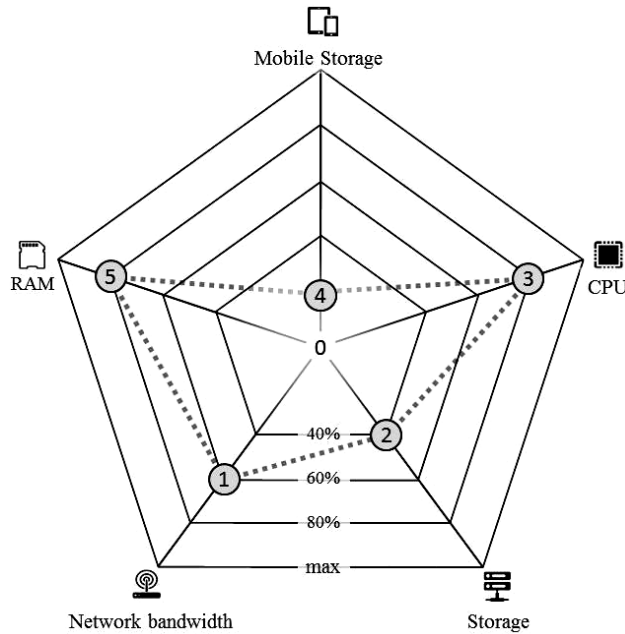
$$P_i = \frac{1}{n} \sum_{i=1}^{n} T_i.$$

Puc. 2. Data center service resources occupancy radar chart

Prediction technique is based on the fuzzy nearness category that use input values of STI and SROI values dynamic changes (as a real time process). A fuzzy matching algorithm estimates the nearness degree of STI and SROI of the prediction time. The nearness level of STI values' dataset (X_n) and SROI values' dataset (Y_n) for the n time moments to be predicted should be estimated to X_i and Y_i that the closest ones to X_n and Y_n, respectively. To calculate SPI values' dataset as a set of predicted performance values at predicted n time moments, X_i and Y_i values have to be used (Fig. 3).

Estimation of SPI values' dataset is impossible without getting the nearness degree of STI and SROI which is based on calculating of the membership degree (Figure 3). The membership degree is a value of membership function $F \in [0;100\%]$ that refers to the correlations between an element and some characteristic [1, 9]. The calculation of a membership function is based on eigenvalue matrix of X_i and Y_i datasets:

$$\begin{cases} F(X_i) = \dfrac{X_i - \min(X_n)}{\max(X_n) - \min(X_n)}; \\ F(Y_i) = \dfrac{Y_i - \min(Y_n)}{\max(Y_n) - \min(Y_n)}. \end{cases}$$

It allows obtaining fuzzy matrix of $F(X_i)$ and c $F(Y_i)$ datasets (Fig. 3). Together with $F(X_n)$ and $F(Y_n)$ datasets it should be used to obtain the nearness degree:

$$ND(A_i, A_n) = ((F(X_i) \vee F(X_N))) \wedge (((1 - F(X_i)) \wedge (1 - F(X_N))) \vee$$

$$\vee((1 - F(Y_i)) \wedge (1 - F(Y_N)))),$$

where A_i represents the matrix in moment i (an estimated moment of time), and A_n represents the matrix in moment n (a predicted moment of time).
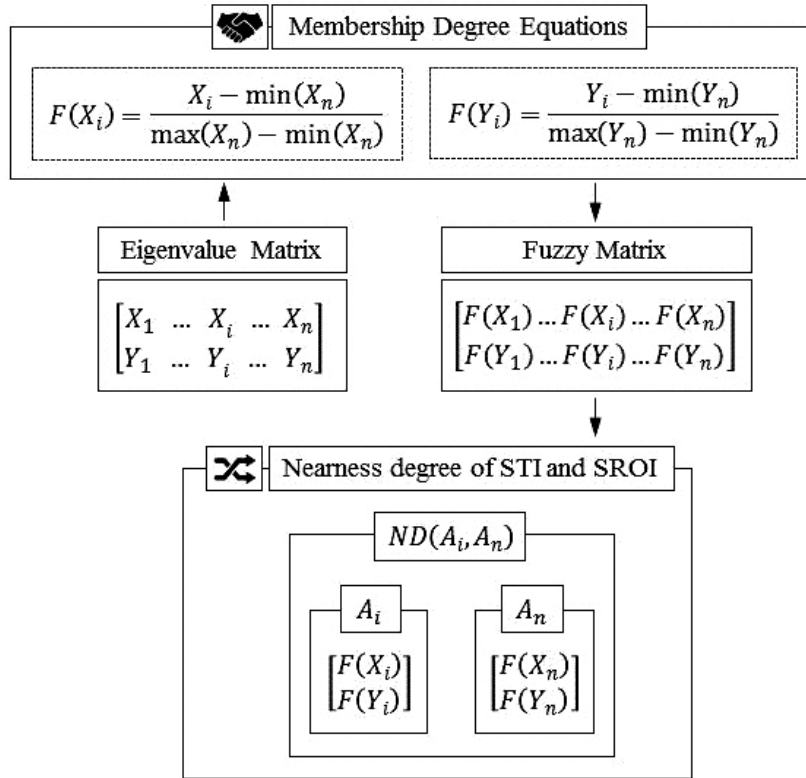

Fig. 3. Evaluation of nearness degree of STI and SROI.

CONCLUSIONS

Main stages of data center service performance prediction, such as indicators' data monitoring and gathering, calculation and prediction of key indexes of data center infrastructure work and performance index prediction were discussed. It was proposed to build the data center service performance prediction algorithm based on an analysis of the service transactions index, service resource occupancy index and service performance index. The prediction of the indexes was based on the chaotic time series analysis that was used to estimate the service transactions index time series trend, radar chart method to calculate the service resource occupancy index value and weighted average method to calculate the service performance index.

For performance prediction, it was proposed to use the fuzzy judgment matrix with the service transactions index and service resource occupancy index as input values. Next stages include the definition of a fuzzy closeness degree and an estimation of the best matching value of the indexes at the predicted moment by the similarity matching algorithm. It was taken into consideration that service

transactions index is usually represented by nonlinear time series. It was noticed that the index time series parameters have to be predicted by the chaos theory and thereby for the calculation of this index the estimation procedure of Lyapunov exponent value was used. Radar chart that was used for service resource occupancy index estimation was built for five main resources of the cloud platform service: shared storage, mobile storage, memory, computational capability and network bandwidth. For calculation of service performance index values' dataset it is necessary to find the nearness degree of the service transactions index and service resource occupancy index; it was proposed to estimate the first membership degree. Therefore, the prediction technique was based on the fuzzy nearness category that used input values of service transactions index and service resource occupancy index dynamic changes which was considered as a real time process.

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