

**HYBRID SYSTEM OF COMPUTATIONAL INTELLIGENCE
BASED ON BAGGING AND GROUP METHOD
OF DATA HANDLING**

Ye. BODYANSKIY, O. KUZMENKO, He. ZAICHENKO, Yu. ZAYCHENKO

Abstract. The paper considers the problem of short- and middle-term forecasting in the financial sphere. To solve this problem, a hybrid system of computational intelligence based on the group method of data handling (GMDH) and bagging, as well as an algorithm for its training, is proposed. The odd stacks of the hybrid system are formed by ensembles of parallel connected subsystems. ARIMA and the GMDH-neo-fuzzy hybrid network were chosen as such subsystems. The proposed system does not require a large training data set, automatically determines the number of stacks during training, and provides online operation. The experimental investigations were conducted using the proposed hybrid system, as well as separately using ARIMA and GMDH-neo-fuzzy. The accuracy of the predictions obtained is compared, based on which the feasibility of using the proposed hybrid system is substantiated.

Keywords: hybrid system, bagging, hybrid GMDH-neo-fuzzy network, ARIMA, short- and middle-term forecasting.

INTRODUCTION

Today deep neural networks (DNN) are widely used for solving a large class of Data mining problems and, above all, classification (pattern recognition, image processing of various nature) and extrapolation (time series forecasting, natural language text processing, fault detection), due to their universal approximating properties, based mainly on the G. Cybenko [2] theorem. At the same time, DNNs are rather cumbersome constructs that contain too many configurable synaptic weights, in turn, requiring too much training data, which is not always available for solving specific real-world problems. In addition, the learning process of DNN requires quite a lot of time so that when solving Data Stream mining problems, especially when processing nonstationary data streams, the use of these systems encounters some difficulties.

It is possible to overcome these difficulties using ensemble methods [2–7], while the ensemble can contain a variety of computational intelligence systems the simplest type of elementary perceptron of F. Rosenblatt and N – Adaline [8] to the most complex DNNs.

The main problem when using the ensemble approach is to combine the results of individual members of this ensemble in order to obtain the optimal initial result in the sensing of the accepted learning criterion. For this purpose, Bagging procedures [9] can be used, minimizing the RMS error on the training sample, modified to work online.

The resulting ensemble approach and bagging system may be too complex from a computational point of view. To simplify its implementation, it should be decomposed into a number of simpler subsystems, while such decomposition can be implemented quite simply using the Group Method of Data Handling (GMDH) [10; 11].

It is interesting to note that J. Schmidhuber [12] believes that just based on GMDH the first deep learning systems were built. Subsequently, based on GMDH, neural networks and neuro-fuzzy systems were proposed, which demonstrated their accuracy and speed in solving a number of problems [13–17].

In our opinion, it is appropriate to introduce into consideration a hybrid system of computational intelligence (HSCI), built based on an ensemble approach and bagging, which would increase its architecture in the learning process based on GMDH ideas, would not require significant amounts of training selections and would be quite simple from a computational point of view.

ARCHITECTURE OF HSCI ON THE BASE OF BAGGING AND GMDH

In the Fig. 1 the architecture of the proposed system is presented.

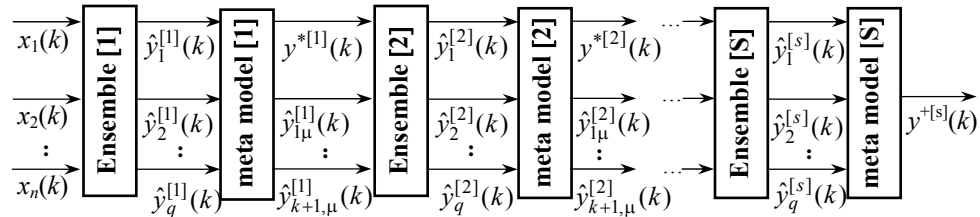


Fig. 1. Hybrid system of computational intelligence based on bagging and GMDH

The architecture of the system contains 2S sequentially-connected stacks, while odd stacks are formed by ensembles of parallel-connected subsystems that solve the same problem (recognition, prediction, etc.) and even ones are essentially learning metamodells that generalize the output signals of ensembles and form optimal results in the sense of the accepted criterion. The output signal of the first metamodell is the generalized optimal signal $y^{*1}(k)$ and $(n-1)$ output signals $\hat{y}_{i\mu}^{[1]}(k)$, $i=1,2,\dots,n-1(k)$ “best members of the ensemble”. At their core, metamodells function as selection units in traditional GMDH systems, but not only select the best results from the previous stack, but also form the optimal solution based on these results.

Further, the output signals of the first metamodell are fed to the inputs of the second ensemble, which is completely similar to the first. The outputs of the second ensemble $\hat{y}_1^{[2]}(k), \hat{y}_2^{[2]}(k), \dots, \hat{y}_q^{[2]}(k)$ come to the second metamodell, which calculates the optimal signal $y^{*2}(k)$ and $(n-1)\hat{y}_{i\mu}^{[2]}(k)$ “closest” to it. The last S-th ensemble is similar to the first two, and the output of the last S-th metamodell

is $y^{*[s]}(k)$, which exactly corresponds to a priori established requirements for the quality of solving the problem under consideration.

Each of the ensembles contains q different computational intelligence systems that solve the same problem. There may still be simple neural networks such as a single-layer perceptron, radial-basis neural network (RBFN), counterpropagating neural network, etc., which do not use error backpropagation procedure for training, neuro-fuzzy systems such as ANFIS, Wang-Mendel or Takagi-Sugeno-Kang type, wavelet-neuro systems, neo-fuzzy neurons and others, the output signal of which linearly depends on the adapted parameters, which allows to use optimal speed learning algorithms.

LEARNING HSCI BASED ON BAGGING AND GMDH

The input information, on the basis of which the system is configured, is a training selection of input signals $x(1), x(2), \dots, x(k), \dots, x(N)$; $x(k) = (x_1(k), \dots, x_i(k), \dots, x_n(k))^T \in R^n$ and its corresponding scalar reference signals $y(1), \dots, y(k), \dots, y(N)$. On the basis of these observations, the elements of the first ensemble are tuned independently of each other, at the outputs of which q scalar signals $y_p^{[2]}(k)$, $p = 1, 2, \dots, q$, are formed, which are conveniently represented in the form of a vector $\hat{y}^{[1]}(k) = (\hat{y}_1^{[1]}(k), \dots, \hat{y}_p^{[1]}(k), \dots, \hat{y}_q^{[1]}(k))^T$. These signals are sent to the inputs of the first metamodel, at the outputs of which n sequences $\hat{y}^{*[1]}(k), \hat{y}_{1\mu}^{[1]}(k), \dots, \hat{y}_{i\mu}^{[1]}(k), \dots, \hat{y}_{n-1,\mu}^{[1]}(k)$ the main of which is $\hat{y}^{*[1]}(k)$ while others are auxiliary. The main signal of the metamodel $y^{*[1]}(k)$ is the union of the outputs of all members of the ensemble in the form of

$$y^{*[1]}(k) = \sum_{p=1}^q w_p^{*[1]} \hat{y}_p^{[1]}(k) = \hat{y}^{[1]T}(k) w^{*[1]},$$

where $w^{*[1]} = (w_1^{*[1]}, \dots, w_p^{*[1]}, \dots, w_q^{*[1]})^T$ — is a vector of adapted parameters-synaptic weights on which additionally restrictions are set on unbiasedness

$$\sum_{p=1}^q w_p^{*[1]} = I_q^T w^{*[1]} = 1, \quad (1)$$

where I_q — $(q \times 1)$ is the vector of unities.

The problem of teaching the first metamodel is reduced to minimizing the standard quadratic criterion in the presence of additional constraints (1).

Thus, the problem of training the first metamodel can be solved using the standard method of penalty functions, which in this case reduces to minimizing the expression

$$J(w^{*[1]}, \delta) = (Y(N) - \bar{Y}^{[1]}(N) w^{*[1]})^T (Y(N) - \bar{Y}^{[1]}(N) w^{*[1]}) + \delta^{-2} (I_q^T w^{*[1]} - 1), \quad (2)$$

where $Y(N) = (y(1), \dots, y(k), \dots, y(N))^T - (N \times 1)$ is a vector, $\bar{Y}^{[1]}(N) = (\hat{y}^{[1]}(1), \dots, \hat{y}^{[1]}(k), \dots, \hat{y}^{[1]}(N))^T - (N \times q)$ is a matrix, δ is the penalty coefficient.

Minimization (2) by $w^{*[1]}$ leads to the result

$$w^{*[1]} = \lim_{\delta \rightarrow 0} w^1(\delta) = w^{LS[1]} + P^{[1]}(N) \frac{1 - I_q^T w^{LS[1]}}{I_q^T P^{[1]}(N) I_q} I_q, \quad (3)$$

where $w^{LS[1]}$ is a standard LSM estimate:

$$w^{LS[1]} = (\bar{Y}^{[1]T}(N) \bar{Y}^{[1]}(N))^+ \bar{Y}^{[1]T}(N) Y(N) = P^{[1]}(N) \bar{Y}^{[1]T}(N) Y(N).$$

The same result may be obtained using the indefinite Lagrange multipliers.

Introducing into consideration meta-model error

$$\begin{aligned} e^{[1]}(k) &= y(k) - y^{*[1]}(k) = y(k) - \hat{y}^{[1]T}(k) w^{*[1]} = w^{*[1]T} I_q y(k) - w^{*[1]T} \hat{y}^{[1]T}(k) = \\ &= w^{*[1]T} (I_q y(k) - \hat{y}^{[1]}(k)) = w^{*[1]T} E^{[1]}(k), \end{aligned}$$

write Lagrange function in the form

$$\begin{aligned} L(w^{*[1]}, \lambda) &= \\ &= \sum_{k=1}^N w^{*[1]T} E^{[1]}(k) E^{[1]T}(k) w^{*[1]} + (I_q^T w^{*[1]} - 1) = w^{*[1]T} R(N) w^{*[1]} + \lambda (I_q^T w^{*[1]} - 1), \end{aligned}$$

(where λ is indefinite Lagrange multiplier) and solving Kuhn–Tucker equations system

$$\begin{cases} \bar{w}_{w^{*[1]}} L(w^{*[1]}, \lambda) = 2R(N) w^{*[1]} + \lambda I_q = \vec{0}, \\ \partial L(w^{*[1]}, \lambda) / \partial \lambda = I_q^T w^{*[1]} - 1 = 0, \end{cases}$$

obtain the final result

$$\begin{cases} w^{*[1]} = R^{-1}(N) I_q (I_q^T R^{-1}(N) I_q)^{-1}, \\ \lambda = -2 I_q^T R^{-1}(N) I_q. \end{cases}$$

It was proved [3; 4] that the use of score (3) leads to results that are not inferior in accuracy to the best of the members of the first ensemble.

If observations from the training sample are processed sequentially online, it is advisable to use the least squares recurrent method in the form

$$\begin{cases} P^{[1]}(k+1) = P^{[1]}(k) - \frac{P^{[1]}(k) \hat{y}^{[1]}(k+1) \hat{y}^{[1]T}(k+1) P^{[1]}(k)}{1 + \hat{y}^{[1]T}(k+1) P^{[1]}(k) \hat{y}^{[1]}(k+1)}, \\ w^{LS[1]}(k+1) = w^{LS[1]}(k) + P^{[1]}(k+1) (y(k+1) - \hat{y}^{[1]T}(k+1) w^{LS[1]}(k) \hat{y}^{[1]}(k+1)), \\ w^{*[1]}(k+1) = w^{LS[1]}(k+1) + P^{[1]}(k+1) (I_q^T P^{[1]}(k+1) I_q)^{-1} (1 - I_q^T w^{LS[1]}(k+1) I_q), \\ w_p^*(0) = q^{-1} \quad p = 1, 2, \dots, q \end{cases}$$

or if a training sample is non-stationary we may use exponentially weighted recurrent LSM method

$$\begin{cases} P^{[1]}(k+1) = \frac{1}{\alpha} \left(P^{[1]}(k) - \frac{P^{[1]}(k) \hat{y}^{[1]}(k+1) \hat{y}^{[1]T}(k+1) P^{[1]}(k)}{\alpha + \hat{y}^{[1]T}(k+1) P^{[1]}(k) \hat{y}^{[1]}(k+1)} \right), \\ w^{LS[1]}(k+1) = w^{LS[1]}(k) + \frac{P^{[1]}(k) (y(k+1) - \hat{y}^{[1]T}(k+1) w^{LS[1]}(k) \hat{y}^{[1]}(k+1))}{\alpha + \hat{y}^{[1]T}(k+1) P^{[1]}(k) \hat{y}^{[1]}(k+1)} \hat{y}^{[1]}(k+1), \\ w^{*[1]}(k+1) = w^{LS[1]}(k+1) + P^{[1]}(k+1) (I_q^T P^{[1]}(k+1) I_q)^{-1} (1 - I_q^T w^{LS[1]}(k+1) I_q), \\ w_p^*(0) = q^{-1} \quad p = 1, 2, \dots, q, \end{cases}$$

quently in the form of $(n \times 1)$ — vector are fed to the input of the second ensemble, the outputs of which go to the inputs of the second metamodel, and so on. The process of increasing the number of ensembles and metamodels continues until the required accuracy of the last metamodel with the output $y^{*[s]}(k)$ is achieved, or the value of the criterion minimized for the bagging model begins to increase, i.e. $\bar{\varepsilon}^2(y^{*[s+1]}(k)) \geq \bar{\varepsilon}^2(y^{*[s]}(k))$.

EXPERIMENTAL INVESTIGATIONS

The experimental investigations of bagging based on GMDH were performed at the problems of short-term and middle-term forecasting of Dow–Jones Industrial average index. The dynamics of DJIA is presented in the Fig. 2.

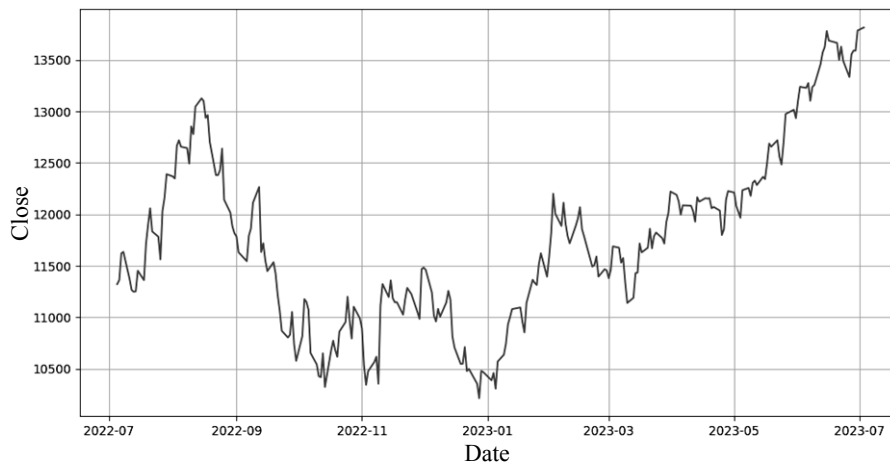


Fig. 2. Dynamics of Dow–Jones Average

The data of DJ index was taken since 05.07.22 till 03.07.23.

The correlation function of process Dow–Jones index was calculated and the correlogram was built presented in the Fig. 3.

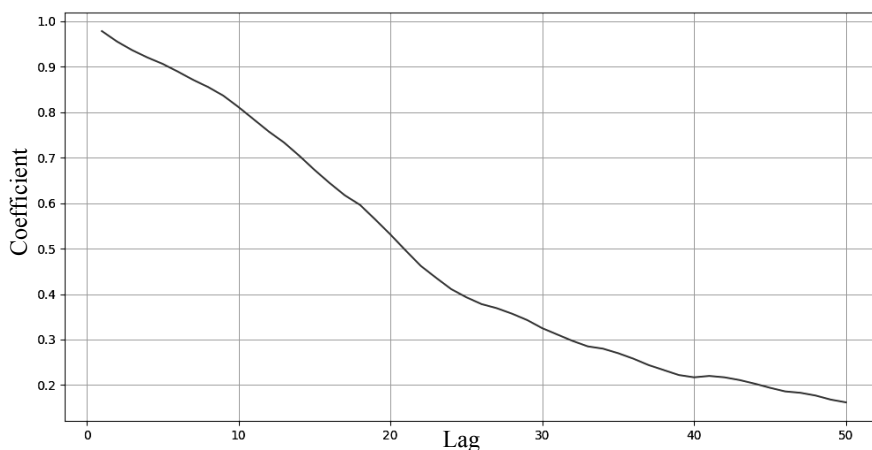


Fig. 3. Correlogram

Analyzing this correlogram we can see strong correlation between values of DJIA.

As a first model used in bagging ensemble is ARIMA. ACF function plot is presented in the Fig. 4.

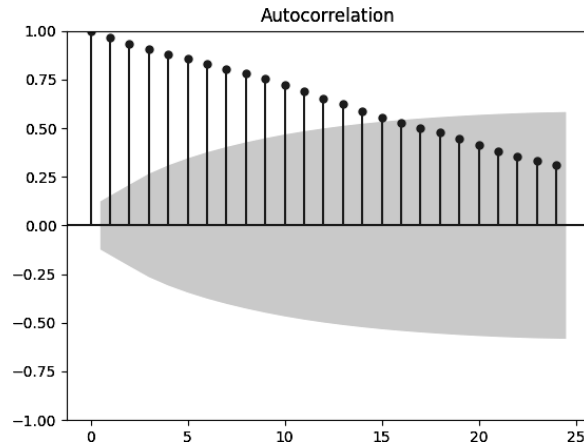


Fig. 4. ACF plot

Using differencing the process DJIA was transformed to stationary one:

Dickey–Fuller test was performed: P -value: $1.3051439086544856e-28 < 0.05$.

The experimental investigations were performed at different forecasting intervals: 1, 3, 5 (short-term) and 10, 20 days (middle-term) forecasting.

Flow-chart for 1 day forecast is presented in the Fig. 5.

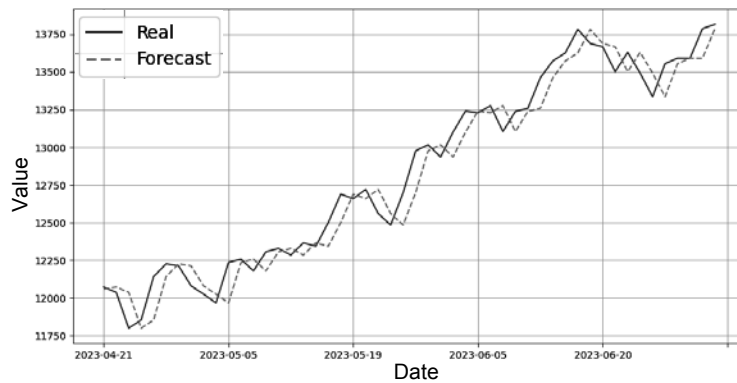


Fig. 5. Flow chart of forecast at 1 day interval for ARIMA

Flow chart of forecast by ARIMA for 5 days is shown in the Fig. 6.

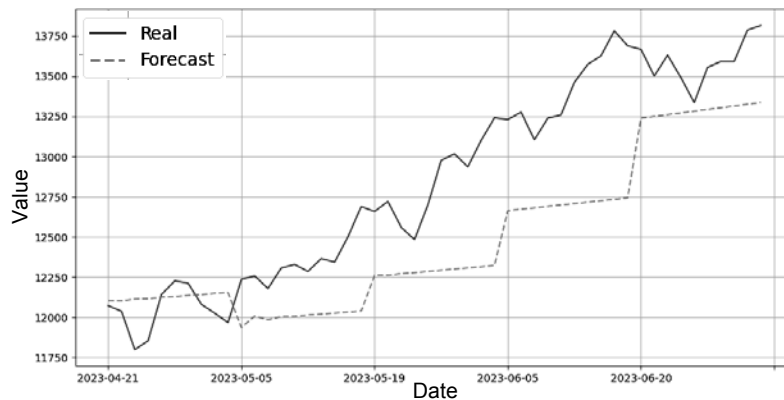


Fig. 6. Flow chart of forecast at 5 days interval for ARIMA

Next model used in ensemble is Hybrid GMDH-neo-fuzzy network. It was optimized by parameters. After that the experiments on forecasting with different forecasting intervals 1, 3, 5, 10, 20 days were performed. Some of results are presented below. Flowchart of forecast for 3 days is shown in the Fig. 7 and for 10 days in the Fig. 8.

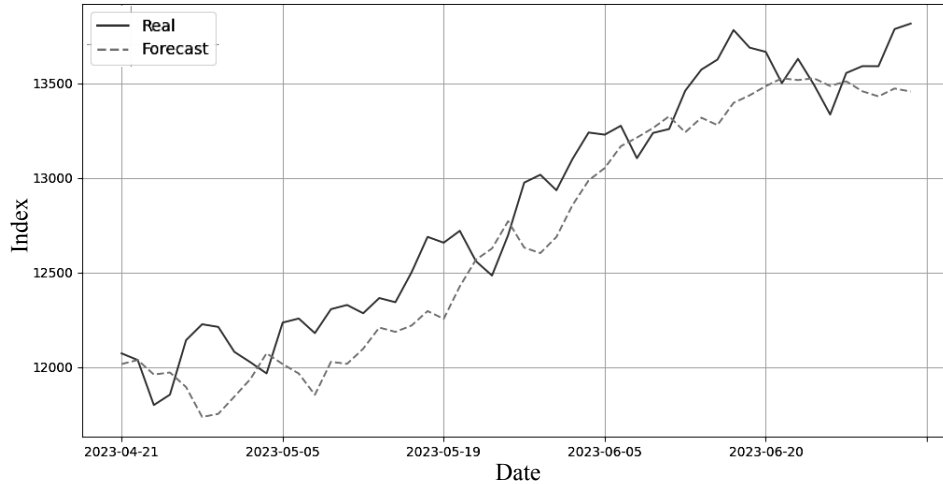


Fig. 7. Flow chart of forecast for 3 days interval by GMDH-neo-fuzzy network

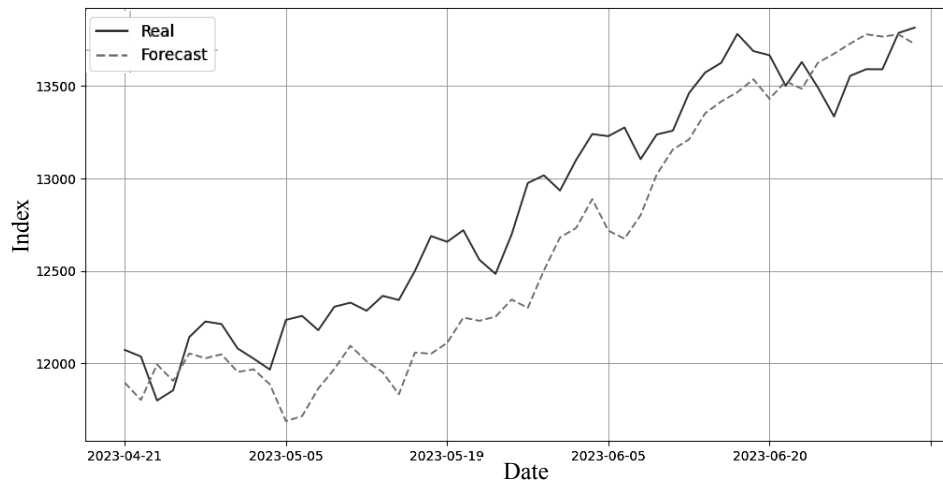


Fig. 8. Flow chart of forecast by GMDH-neo-fuzzy network for 10 days

After that the algorithm of bagging based on GMDH was implemented and experiments at short-term and middle-term forecasting were performed. The tables with criteria MSE and MAPE are presented in the Tables 1 and 2.

Table 1. Average MSE values for different intervals

Interval	ARIMA	GMDH-neo-fuzzy	HSCI-GMDH-bagging
1	17422.752	27420.394	17382.425
3	43434.022	59202.99	49332.635
5	66993.011	78330.284	58153.202
10	235427.989	108358.616	104324.0
20	696291.974	253693.345	241508.146

Table 2. Average MAPE values for different intervals

Interval	ARIMA	GMDH-neo-fuzzy	HSCI-GMDH-bagging
1	0.83	1.049	0.828
3	1.416	1.63	1.398
5	1.616	1.903	1.577
10	3.134	2.208	2.108
20	5.579	3.433	3.308

Average MSE values for different intervals are presented in the Fig. 9 and MAPE values — in the Fig. 10.

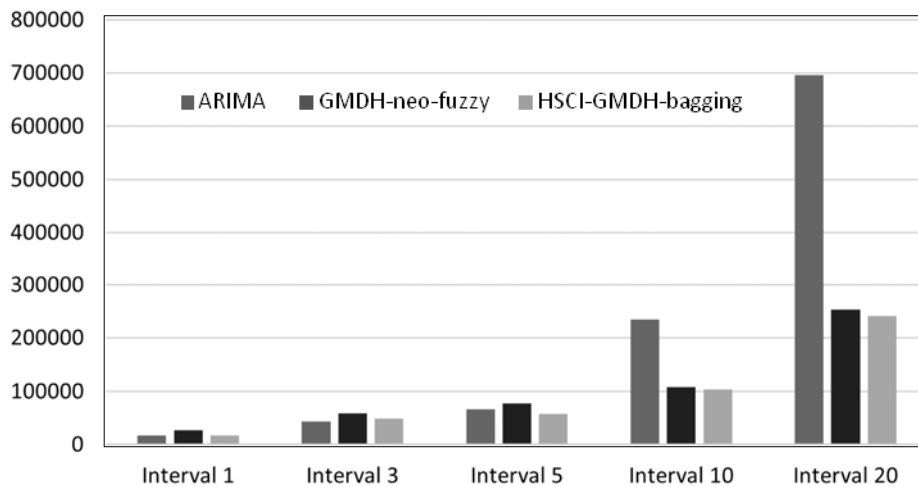


Fig. 9. Average MSE values for different forecasting intervals

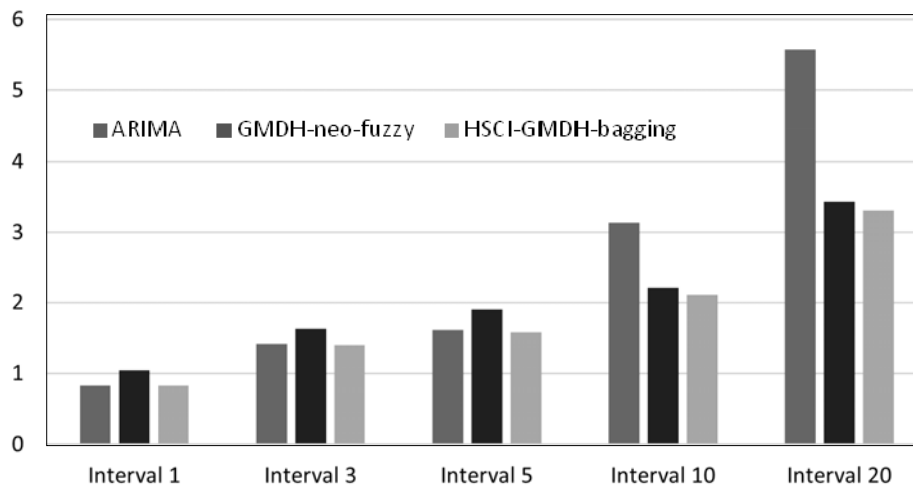


Fig. 10. Average MAPE values for different forecasting intervals

Analyzing the presented results, one may conclude that bagging procedure based on GMDH has the best results as compared with separate models in ensemble, the second place takes GMDH-neo-fuzzy network for all the intervals at the exception 1, 3 and 5 days. And for short-term forecasting 1, 3 and 5 days ARIMA appears to be better than hybrid GMDH-neo-fuzzy network.

In a whole the obtained results well comply with theoretical statements as for properties of bagging procedure and the proposed bagging based on GMDH in HSCI system appeared to be very efficient procedure which demand minimum calculations due to application of GMDH.

CONCLUSION

The architecture and learning algorithms of hybrid computational intelligence system, which is built based on Group Method of Data Handling (GMDH) method and bagging approach, are proposed.

The system consists of a sequence of stacks, while odd stacks are essentially ensembles formed by parallel connected different subsystems that solve the same problem, while even ones are metamodels that implement the bagging procedure and calculate the levels of fuzzy membership of each member of the ensemble to the optimal result. The process of increasing the number of stacks is based on GMDH principles until the desired accuracy of the final results is achieved. The proposed system does not require large volumes of training samples, provides online work and automatically determines the number of its layers — stacks in the learning process.

Experimental investigations confirm that Hybrid system of computational intelligence based on bagging and GMDH is effective for short- and middle-term forecasting in the financial sphere and has better metrics than ARIMA and GMDH neo fuzzy.

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INFORMATION ON THE ARTICLE

Yevgeniy V. Bodyanskiy, ORCID: 0000-0001-5418-2143, Kharkiv National University of Radio Electronics, Ukraine, e-mail: yevgeniy.bodyanskiy@nure.ua

Oleksii V. Kuzmenko, ORCID: 0000-0003-1581-6224, Educational and Research Institute for Applied System Analysis of the National Technical University of Ukraine "Igor Sikorsky Kyiv Polytechnic Institute", Ukraine, e-mail: oleksii.kuzmenko@ukr.net

Helen Yu. Zaichenko, ORCID: 0000-0002-4630-5155, Educational and Research Institute for Applied System Analysis of the National Technical University of Ukraine "Igor Sikorsky Kyiv Polytechnic Institute", Ukraine, e-mail: syncmaster@bigmir.net

Yuriy P. Zaychenko, ORCID: 0000-0001-9662-3269, Educational and Research Institute for Applied System Analysis of the National Technical University of Ukraine "Igor Sikorsky Kyiv Polytechnic Institute", Ukraine, e-mail: zaychenkoyuri@ukr.net

ГІБРИДНА СИСТЕМА ОБЧИСЛЮВАЛЬНОГО ІНТЕЛЕКТУ НА ОСНОВІ БЕГГІНГУ ТА МЕТОДУ ГРУПОВОГО УРАХУВАННЯ АРГУМЕНТІВ / С.В.Бодяньський, О.В. Кузьменко, Ю.П. Зайченко, О.Ю. Зайченко

Анотація. Розглянуто проблему короткострокового та середньострокового прогнозування у фінансовій сфері. Для її вирішення запропоновано гібридну систему обчислювального інтелекту на основі методу групового урахування аргументів (МГУА) та беггінгу, а також алгоритм її навчання. Непарні стеки гібридної системи сформовані ансамблями паралельно з'єднаних підсистем. Як такі підсистеми обрано ARIMA та гібридну мережу МГУА-нео-фаззі. Запропонована система не потребує великого обсягу навчальної вибірки, автоматично визначає кількість стеків у процесі навчання та забезпечує роботу у режимі online. Проведено експериментальні дослідження з використанням запропонованої гібридної системи, а також окремо ARIMA та МГУА-нео-фаззі. Порівняно точність прогнозів, отриманих експериментальним шляхом, на основі чого обґрунтовано доцільність застосування запропонованої гібридної системи.

Ключові слова: гібридна система, беггінг, гібридна мережа МГУА-нео-фаззі, ARIMA, короткострокове та середньострокове прогнозування.